## Dangling Bond Defects at Si-SiO<sub>2</sub> Interfaces: Atomic Structure of the P<sub>b1</sub> Center

András Stirling,<sup>1,2</sup> Alfredo Pasquarello,<sup>1,3</sup> J.-C. Charlier,<sup>1,4</sup> and Roberto Car<sup>1,5</sup>

<sup>1</sup>Institut Romand de Recherche Numérique en Physique des Matériaux (IRRMA), PPH-Ecublens, CH-1015 Lausanne, Switzerland

<sup>2</sup>Institute of Isotope and Surface Chemistry, Budapest, P.O. Box 77, H-1525, Hungary

<sup>3</sup>Ecole Polytechnique Fédérale de Lausanne (EPFL), PPH-Ecublens, CH-1015 Lausanne, Switzerland

<sup>4</sup>Unité de Physico-Chimie et de Physique des Matériaux, Université Catholique de Louvain,

1 Place Croix du Sud, B-1348 Louvain-la-Neuve, Belgium

<sup>5</sup>Department of Chemistry and Princeton Materials Institute, Princeton University, Princeton, New Jersey 08544-1009

(Received 3 March 2000)

Using a first-principles approach, we characterize dangling bond defects at Si-SiO<sub>2</sub> interfaces by calculating hyperfine parameters for several relaxed structures. Interface models, in which defect Si atoms remain close to crystalline sites of the substrate upon relaxation, successfully describe  $P_b$  and  $P_{b0}$  defects at (111) and (100) interfaces, respectively. On the basis of calculated hyperfine parameters, we discard models of the  $P_{b1}$  defect containing a first neighbor shell with an O atom or a strained bond. A novel model consisting of an asymmetrically oxidized dimer yields hyperfine parameters in excellent agreement with experiment and is proposed as the structure of the  $P_{b1}$  center.

PACS numbers: 68.35.Dv, 61.72.Ji, 76.30.Mi

Intrinsic defects at Si-SiO<sub>2</sub> interfaces have been intensively investigated for several decades in view of their importance for the operation of metal-oxide-semiconductor devices [1-18]. Unsaturated dangling bonds, generically referred to as  $P_b$ -type centers, occur at the interface between the Si substrate and the oxide and are detected by ESR techniques [1-12]. The proper  $P_h$  center is found at (111) interfaces [1,2], while two distinct defects, referred to as  $P_{b0}$  and  $P_{b1}$ , are distinguished at (100) interfaces [3]. The  $P_b$  center has a clear microscopic characterization as an isolated  $sp^3$  dangling bond of the substrate pointing into the (111) direction, orthogonal to the interface [2]. Its identification as a  ${}^{\bullet}Si \equiv Si_3$  unit [2] has firmly been established by the good agreement between measured [5] and calculated hyperfine interactions [13-17]. (The dot represents the lone electron of the defect.) At the technologically relevant (100) interface, such a clear assessment has long been hindered by the experimental resolution related to the lower density of defects at this interface [9]. The axial symmetry of the g matrix, the dangling bond axis along (111), and the overall similarity of the salient ESR data strongly suggest that the  $P_{b0}$  and  $P_b$  centers are chemically identical [6-8]. However, specific modeling of the  $P_{b0}$  defect has so far been missing.

The atomic structure of the  $P_{b1}$  center is more mysterious. Unlike for  $P_b$  and  $P_{b0}$ , the g matrix of  $P_{b1}$  is triclinic [3,8]. Because (111) still is one of the principal directions, it was initially assumed that the local atomic structure of  $P_{b1}$  only marginally differed from that of  $P_b$  or  $P_{b0}$ . Models were put forward in which the symmetry in the nearest neighbor shell is either broken by an O atom [3] or a strained bond [15]. However, neither of these models explains the ambiguous role of oxygen in the  $P_{b1}$  center. On one hand, hyperfine measurements using <sup>17</sup>O rule out its occurrence in the immediate vicinity of the defect [10]. On the other hand, ESR measurements on the Si(100)-Si<sub>3</sub>N<sub>4</sub> interface detected only the  $P_{b0}$  line, strongly suggesting that O atoms might play a critical role in the formation of the  $P_{b1}$  defect [12].

A breakthrough in the characterization of the  $P_{b1}$  defect was recently achieved when its full hyperfine structure was uncovered [9]. The hyperfine tensor revealed that the axis of the dangling bond is oriented close to a (112) direction. Because this orientation does not correspond to a natural bonding direction in crystalline silicon, the  $P_{b1}$  defect must result from an important structural reconstruction at the interface. These puzzling experimental data now call for theoretical modeling to disclose the atomic structure of the  $P_{b1}$  center [9].

In this paper, we set out to determine the atomic structures of  $P_b$ -type defects at Si-SiO<sub>2</sub> interfaces. Using a first-principles approach, we generated several relaxed model structures for which we calculated hyperfine parameters. First, we assessed the accuracy of our scheme by considering the  $P_b$  center for which the atomic structure is well established. Then, we constructed a model at the Si(001)-SiO<sub>2</sub> interface for the  $P_{b0}$  center. In both cases, we obtained excellent agreement with experiment. Finally, we found that models of the  $P_{b1}$  defect suggested so far [18] do not account satisfactorily for the experimental hyperfine data. Instead, a novel model structure, which consists of an asymmetrically oxidized dimer (AOD), yields excellent agreement with experiment and is proposed here as the atomic structure of the  $P_{b1}$  center.

We model Si-SiO<sub>2</sub> interfaces with periodically repeated crystalline slabs. Structural relaxations were performed with a damped molecular dynamics approach [19,20]. The interatomic forces were treated self-consistently within density functional theory in its spin unrestricted version using a generalized gradient approximation for the exchange and correlation energy [21]. We adopt a planewave pseudopotential (PP) approach, with ultrasoft PPs

for both O and Si atoms [22]. Good convergence in the calculated properties is achieved using cutoffs of 25 and 150 Ry for the valence wave functions and the augmented charge density, respectively [20]. The Brillouin zone of the supercells is sampled at the  $\Gamma$  point. A detailed description of our method is given in Ref. [20].

The hyperfine interaction of the  $P_b$  defects is described by the Hamiltonian  $H = \mathbf{I} \cdot \mathbf{A} \cdot \mathbf{S}$ , where the hyperfine tensor **A** describes the coupling between electronic (S = 1/2) and nuclear spins (I = 1/2 for <sup>29</sup>Si). The components of **A** are given by  $A_{ij} = a\delta_{ij} + b_{ij}$ , where

$$a = \frac{8\pi}{3} g_e \mu_e g_{\rm Si} \mu_{\rm Si} \rho_s(\mathbf{R}), \qquad (1)$$

$$b_{ij} = g_e \mu_e g_{\mathrm{Si}} \mu_{\mathrm{Si}} \int \rho_s(\mathbf{r}) \frac{3r_i r_j - \delta_{ij} r^2}{r^5} d^3 \mathbf{r} \,. \tag{2}$$

Here,  $\rho_s = \rho_{\uparrow} - \rho_{\downarrow}$  is the electron spin density,  $g_e$  is the free-electron g factor,  $\mu_e$  is the Bohr magneton,  $g_{Si}$  is the nuclear gyromagnetic ratio for Si,  $\mu_{Si}$  is the corresponding nuclear magneton, and the position vector  $\mathbf{r}$  is given with respect to the nuclear site  $\mathbf{R}$ . The isotropic contribution a to the hyperfine tensor corresponds to the Fermi contact interaction, whereas the anisotropic contribution  $b_{ij}$  results from dipole-dipole interactions. Diagonalization of the matrix  $A_{ij}$  gives the hyperfine splittings and the principal directions. For  $sp^3$  dangling bonds, the matrix  $A_{ij}$  is close to axial symmetry and is fully characterized by the axial direction, the isotropic parameter a, and a single anisotropic parameter b. Its distinct eigenvalues are given by  $A_{\parallel} = a + 2b$  and  $A_{\perp} = a - b$ .

The calculation of  $A_{ij}$  requires the electron spin density in the core region which is not directly available in a PP calculation. However, within the ultrasoft PP scheme [20,22] adopted here the charge density in the core region can easily be reconstructed from the pseudo wave functions  $\phi_i$  and the projector functions  $\beta_n^I$ , using

$$\rho(\mathbf{r}) = \sum_{i} \left[ |\phi_{i}(\mathbf{r})|^{2} + \sum_{nm,I} Q_{nm}^{I}(\mathbf{r}) \langle \phi_{i} | \beta_{n}^{I} \rangle \langle \beta_{m}^{I} | \phi_{i} \rangle \right]$$
(3)

and replacing the soft augmentation functions  $Q_{nm}^{I}(\mathbf{r})$  used in the actual calculation with their original counterparts [20]. We demonstrated the accuracy of this procedure for the Si atom, for which all-electron and reconstructed charge densities are found to be very close, with a maximal error of 2% at the nucleus. Applying a similar reconstruction procedure [23], we successfully determined hyperfine interactions for the  $E'_1$  center in  $\alpha$  quartz [24].

We first consider the  $P_b$  center at the Si(111)-SiO<sub>2</sub> interface, a defect whose atomic structure is well established [13–15,17]. We constructed a periodic interface model by attaching the oxide structure proposed in Ref. [13] to Si(111) (see Fig. 1). The substrate was described by six layers of Si with 12 atoms per layer. We chose the central Si atom under the SiO<sub>2</sub> ring as the defect site, the remaining surface Si atoms being terminated by OH groups. The calculated and measured hyperfine parameters are compared in Table I. The calculated isotropic interaction is

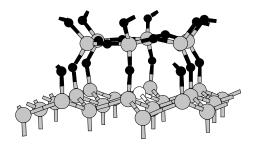


FIG. 1. Relaxed model structure for  $P_b$ .

~20% larger than in experiment, while the anisotropic term is underestimated by ~30%. For hyperfine parameters, this kind of agreement should be considered very good [23,24]. For comparison, the *a* and *b* values reported by Cook and White [13] overestimate the experimental data by 35% and 55%, respectively [25]. The overestimation of the contact interaction in our calculations is affected by the neglect of core polarization. By performing an all-electron calculation [26] on a Si(SiH<sub>3</sub>)<sub>3</sub> model cluster, we found the core contribution to be negative and as large as 10% of the valence contribution [27]. This correction noticeably improves the accord with experiment. The residual error should be attributed to limitations of the exchange-correlation functional [28].

To address  $P_{b0}$  and  $P_{b1}$  defects, we modeled the Si(100)-SiO<sub>2</sub> interface by attaching tridymite, a crystalline form of SiO<sub>2</sub>, to Si(100) [29]. The adopted supercell corresponds to a  $\sqrt{8} \times \sqrt{8}$  repeat unit in the plane of the interface and contains 6 monolayers of Si and 5 layers of SiO<sub>2</sub>. The bond density mismatch at the interface was accommodated by forming Si dimers or by the introduction of O bridges, which eliminated all residual dangling bonds [29]. Defect sites were then generated by appropriate removal of selected atoms. The undesired dangling bonds created by this procedure were saturated with H atoms. The extra H atoms are sufficiently far located from the defect site, such that their influence on the hyperfine parameters is negligible.

Following indications from experimental work [6–8], we considered as a model for  $P_{b0}$  a Si atom regularly

TABLE I. Theoretical and experimental hyperfine values (in  $10^{-4}$  cm<sup>-1</sup>) and dangling bond orientations for  $P_b$ -type centers. Experiment from Ref. [9]. For  $P_{b1}$  we give only the azimuthal angles with the normal of the interface plane, the polar angles being very close to the measured directions.

		а	b	$A_{\parallel}$	$A_{\perp}$	hf axis
$P_b$	Theory Expt.	122 105	14 20	$\begin{array}{c} 150\\ 146\pm5 \end{array}$	$\begin{array}{c}107\\85\ \pm\ 8\end{array}$	[111] [111]
$P_{b0}$	Theory Expt.	119 93	14 23	148 139 ± 4	$\begin{array}{c} 105\\ 70\ \pm\ 5\end{array}$	[111] <111>
$P_{b1}$	Dimer Bridge AOD Expt.	118 160 145 119	14 13 15 19	146 187 175 156 ± 3	$104 \\ 147 \\ 129 \\ 100 \pm 4$	21° 30° 33° 32.3° ±3°

incorporated in the substrate lattice and exposing a dangling bond in a (111) direction (Fig. 2). The agreement with experiment is as good as for the  $P_b$  center (Table I). In particular, the hyperfine axis remains very close to the (111) direction also after relaxation. This result provides further evidence in support of the chemical identity between  $P_b$  and  $P_{b0}$ . Notice that we find for  $P_{b0}$  approximately the same relative errors between calculated and measured hyperfine interactions as for  $P_b$ . This supports the systematic character of these errors.

For the  $P_{b1}$  center, we first examined the strained bond model [15] and the O nearest neighbor model [3]. We here describe these models by dimer and bridge structures as shown in Figs. 3(a) and 3(b). In the dimer model, the contact interaction is found to be close to the experimental value (Table I), but one should not be misled by this agreement in view of the systematic tendency of our approach to overestimate the isotropic interaction by ~20%. The low value of the contact term results from the local strain at the defect site which causes a significant distortion from a regular  $sp^3$  configuration (Table II). Furthermore, the calculated hyperfine axis is tilted by more than 10° from the experimental direction [9].

In the bridge model, the orientation of the hyperfine axis agrees well with experiment (Table I). However, the overestimation of the isotropic interaction by about 35% appears too large in view of our results for the similar  $P_b$ and  $P_{b0}$  defects. In the presence of a first-neighbor O atom, the core-polarization correction reduces to 5% [27], concurrently emphasizing the inadequacy of this model. The large value of the contact interaction is a consequence of the large electronegativity of the O neighbor which tends to increase the *p* character of the bonding orbitals. Consequently the *s* character of the unpaired orbital increases [30]. Further arguments against the bridge model come from the <sup>17</sup>O hyperfine experiment [10], which indicate the absence of O atoms in the defect's first-neighbor shell.

The inadequacies of the dimer and the bridge model contribute to defining the requirements that an appropriate model for the  $P_{b1}$  defect should meet: (i) the defect is

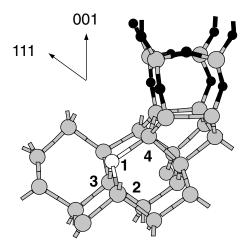


FIG. 2. Relaxed model structure for  $P_{b0}$ .

registered with respect to the underlying silicon substrate, as the dangling bond is experimentally observed to point into well defined directions [8]; (ii) the orientation of the dangling bond with the interface normal is  $32.3^{\circ} \pm 3^{\circ}$  [9]; (iii) oxygen is not part of the defect's core, which is described by a  $\bullet$ Si = Si<sub>3</sub> unit [8–10]; and (iv) the local geometry of the defect Si atom should be close to an ideal  $sp^3$  configuration to give a sufficiently large contact interaction. These constraints led us to consider the asymmetrically oxidized dimer model shown in Fig. 3(c). For this model, the full set of hyperfine parameters is found to agree closely with the experimental data (Table I). The contact interaction is overestimated by 22%, which is completely consistent with the systematic tendency manifested in our calculations. The role of the O atoms in the AOD model elucidates the apparent conflict resulting from experimental data [10,12]. Oxygen atoms are not first neighbors of the defect [10], yet they play a crucial role [12]. First, they tilt the dimer bond in the right direction bringing the axis of the dangling bond within 1° of the experimental direction (Table I). Second, they partially relieve strain out of the dimer structure, yielding an almost ideal  $sp^3$  configuration (Table II). We therefore propose the AOD model as the most likely candidate for the  $P_{b1}$  center. With this identification, the experimental trends in the hyperfine parameters of  $P_{b0}(P_b)$  and  $P_{b1}$  are nicely reproduced by our calculations.

The current understanding of the oxidation mechanism is quite limited and does not allow us to explain the formation process of specific defects at Si-SiO<sub>2</sub> interfaces. Nevertheless, it is suggestive to assemble the results of a series of recent first-principles studies [31-33]. In a

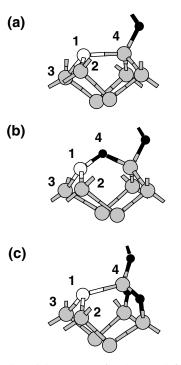


FIG. 3. Relaxed model structures for the  $P_{b1}$  defect: (a) dimer, (b) bridge, and (c) AOD model.

TABLE II. Geometry of the relaxed  $P_b$ -type models. The defect atom is labeled either as  $Si_d$  or  $Si_1$ , the other numbers identify nearest neighbor silicon atoms (cf. Fig. 2).

Defect	Model	Bond ler	ngth (Å)	Bond angle	
$P_b$		Si <sub>d</sub> -Si	2.342	Si-Si <sub>d</sub> -Si	109.9°
$P_{b0}$		$\begin{array}{c} Si_1\text{-}Si_2\\Si_1\text{-}Si_3\\Si_1\text{-}Si_4 \end{array}$	2.344 2.366 2.361	$\begin{array}{c} Si_2 \hbox{-} Si_1 \hbox{-} Si_4 \\ Si_2 \hbox{-} Si_1 \hbox{-} Si_3 \\ Si_3 \hbox{-} Si_1 \hbox{-} Si_4 \end{array}$	108.7° 106.4° 108.4°
$P_{b1}$	Dimer	$\begin{array}{c} Si_1\text{-}Si_2\\Si_1\text{-}Si_3\\Si_1\text{-}Si_4 \end{array}$	2.349 2.331 2.446	$Si_2-Si_1-Si_4$ $Si_2-Si_1-Si_3$ $Si_3-Si_1-Si_4$	109.3° 112.5° 106.5°
	Bridge	$Si_1 - Si_2$ $Si_1 - Si_3$ $Si_1 - O_4$	2.338 2.336 1.662	$Si_2 - Si_1 - O_4$ $Si_2 - Si_1 - O_4$ $Si_2 - Si_1 - Si_3$ $Si_3 - Si_1 - O_4$	102.7° 118.8° 100.9°
	AOD	$\begin{array}{c} Si_1 \cdot Si_2\\ Si_1 \cdot Si_2\\ Si_1 \cdot Si_3\\ Si_1 \cdot Si_4 \end{array}$	2.345 2.370 2.393	$\begin{array}{c} Si_{3} \cdot Si_{1} \cdot Si_{4} \\ Si_{2} \cdot Si_{1} \cdot Si_{3} \\ Si_{3} \cdot Si_{1} \cdot Si_{4} \end{array}$	108.8° 109.2° 110.3°

molecular-dynamics investigation, network relaxation processes occurring during oxidation were shown to yield dimer reconstructions at the buried interface [31]. Energetic studies of dimer-reconstructed Si(001)2  $\times$  1 surfaces identified a preferential channel for backbond oxidation [32]. Subsequent oxidation in the neighboring backbond then becomes energetically convenient [33]. This plausible sequence of atomic processes appears consistent with the formation of AOD structures during oxidation.

The authors acknowledge fruitful interactions with A. Stesmans, G.-M. Rignanese, and F. Mauri. A. S. acknowledges support from the Ministry of Education and from the Hungarian Academy of Sciences within the Eötvös and Bolyai programs. A. P. acknowledges support from the Swiss National Science Foundation within the PROFIL program (Grant No. 21-52'182.97). J. C. C. acknowledges the National Fund for Scientific Research (FNRS) of Belgium for financial support. The calculations were performed on the NEC-SX4 of the Swiss Center for Scientific Computing (CSCS).

- [1] Y. Nishi, Jpn. J. Appl. Phys. 10, 52 (1971).
- [2] P. Caplan, E. Poindexter, B. Deal, and R. Razouk, J. Appl. Phys. 50, 5847 (1979).
- [3] E. H. Poindexter, P. J. Caplan, B. E. Deal, and R. Razouk, J. Appl. Phys. 52, 879 (1981).
- [4] E. H. Poindexter and P. J. Caplan, Prog. Surf. Sci. 14, 201 (1983).
- [5] K.L. Brower, Appl. Phys. Lett. 43, 1111 (1983).
- [6] F. C. Rong, J. F. Harvey, E. H. Poindexter, and G. J. Gerardi, Appl. Phys. Lett. 63, 920 (1993).
- [7] H.J. von Bardeleben, M. Schoisswohl, and J.L. Cantin, Colloids Surf. A 115, 277 (1996).
- [8] A. Stesmans and V. V. Afanas'ev, J. Appl. Phys. 83, 2449 (1998).
- [9] A. Stesmans, B. Nouwen, and V.V. Afanas'ev, J. Phys. Condens. Matter **10**, L465 (1998); Phys. Rev. B **58**, 15 801 (1998).

- [10] K.L. Brower, Z. Phys. Chem. (Leipzig) 151, 177 (1987).
- [11] J.L. Cantin et al., Phys. Rev. B 52, R11 599 (1995).
- [12] P. Aubert et al., Phys. Rev. B 59, 10677 (1999).
- [13] M. Cook and C. T. White, Phys. Rev. Lett. 59, 1741 (1987); Phys. Rev. B 38, 9674 (1988).
- [14] A. H. Edwards, Phys. Rev. B 36, 9638 (1987).
- [15] A.H. Edwards, in *The Physics and Chemistry of SiO<sub>2</sub> and the SiO<sub>2</sub> Interface*, edited by C.R. Helms and B.E. Deal (Plenum, New York, 1988), p. 271.
- [16] J. H. Stathis, E. Cartier, A. H. Edwards, and E. H. Poindexter, in *Silicon Nitride and Silicon Dioxide Thin Insulating Films*, edited by M. J. Deen *et al.* (Electrochemical Society, Pennington, NJ, 1997), p. 259.
- [17] B. Tuttle, Phys. Rev. B 60, 2631 (1999).
- [18] A.H. Edwards and W.B. Fowler, Microelectron. Reliab. 39, 3 (1999).
- [19] R. Car and M. Parrinello, Phys. Rev. Lett. 55, 2471 (1985).
- [20] A. Pasquarello *et al.*, Phys. Rev. Lett. **69**, 1982 (1992);
  K. Laasonen *et al.*, Phys. Rev. B **47**, 10142 (1993).
- [21] J. P. Perdew et al., Phys. Rev. B 46, 6671 (1992).
- [22] D. Vanderbilt, Phys. Rev. B 41, 7892 (1990).
- [23] C. G. Van de Walle and P. E. Blöchl, Phys. Rev. B 47, 4244 (1993).
- [24] M. Boero, A. Pasquarello, J. Sarnthein, and R. Car, Phys. Rev. Lett. 78, 887 (1997).
- [25] Values for the cluster with an oxide (see Ref. [13]).
- [26] M.J. Frisch, G.W. Trucks, H.B. Schlegel, G.E. Scuseria, M.A. Robb, J.R. Cheeseman, V.G. Zakrzewski, J.A. Montgomery, Jr., R.E. Stratmann, J.C. Burant, S. Dapprich, J.M. Millam, A.D. Daniels, K.N. Kudin, M.C. Strain, O. Farkas, J. Tomasi, V. Barone, M. Cossi, R. Cammi, B. Mennucci, C. Pomelli, C. Adamo, S. Clifford, J. Ochterski, G.A. Petersson, P.Y. Ayala, Q. Cui, K. Morokuma, D.K. Malick, A.D. Rabuck, K. Raghavachari, J.B. Foresman, J. Cioslowski, J.V. Ortiz, B.B. Stefanov, G. Liu, A. Liashenko, P. Piskorz, I. Komaromi, R. Gomperts, R.L. Martin, D.J. Fox, T. Keith, M.A. Al-Laham, C.Y. Peng, A. Nanayakkara, C. Gonzalez, M. Challacombe, P.M.W. Gill, B. Johnson, W. Chen, M.W. Wong, J.L. Andres, C. Gonzalez, M. Head-Gordon, E.S. Replogle, and J.A. Pople, GAUSSIAN 98, Revision A.6, Gaussian, Inc., Pittsburgh, PA, 1998.
- [27] By considering Si(SiH<sub>3</sub>)<sub>3-n</sub>(OH)<sub>n</sub> clusters, we found that the core contribution depends on the number of neighbor O atoms: 10% (n = 0), 5% (n = 1), 2% (n = 2), 1% (n = 3).
- [28] V. Barone, in *Recent Advances in Density Functional Methods*, edited by D. P. Chong (World Scientific, Singapore, 1995).
- [29] A. Pasquarello, M. S. Hybertsen, and R. Car, Phys. Rev. Lett. 74, 1024 (1995); Phys. Rev. B 53, 10942 (1996); Appl. Phys. Lett. 68, 625 (1996); Appl. Surf. Sci. 104/ 105, 317 (1996).
- [30] H.A. Bent, Chem. Rev. 61, 275 (1961).
- [31] A. Pasquarello, M. S. Hybertsen, and R. Car, Nature (London) **396**, 58 (1998).
- [32] K. Kato, T. Uda, and K. Terakura, Phys. Rev. Lett. 80, 2000 (1998).
- [33] B. S. Stefanov and K. Raghavachari, Surf. Sci. 389, L1159 (1997).