Spin Tunneling via Dislocations in Mn$_{12}$ Acetate Crystals

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We show that dislocations should be the main source of spin tunneling in Mn$_{12}$ crystals. Long range strains caused by dislocations produce broad distribution of relaxation times that has been seen in many experiments. When the external magnetic field is applied along the c axis of the crystal, local rotations of the magnetic anisotropy axis due to dislocations result in the effective local transverse magnetic field that unfreezes odd tunneling resonances. Scaling law is derived that provides universal description of spin tunneling for all resonances.

Mn$_{12}$ acetate crystals exibit quantum magnetic phenomena at macroscopic scale. They have a centered tetragonal structure with $a = 17.319$ Å and $c = 12.388$ Å as lattice parameters [1,2]. Spin-10 Mn$_{12}$ molecules at the sites of the lattice show magnetic bistablity due to the 65 K barrier between the spin-up and spin-down states [3]. Quantization of spin levels manifests itself in a spectacular stepwise magnetic hysteresis [4]. Other observations include memory effects [5], nonexponential relaxation [5–7], and a peculiar crossover between thermal and quantum behavior [6,8]. Theoretical models explain tunneling in Mn$_{12}$ by phonons [9–11], nuclear spins, dipolar fields, fourth-order magnetic anisotropy [12], Landau-Zener effect, etc. Explanation of some observations remains controversial though.

First, there is no agreement among researchers on what causes tunneling in Mn$_{12}$. The fourth-order transverse anisotropy cannot account for odd resonances. Besides, it is too weak, as are hyperfine and dipolar fields, to provide the actual tunneling rate. Second, the time dependence of the magnetic relaxation in Mn$_{12}$ has not been understood. If all Mn$_{12}$ molecules were subject to the same crystal field, the magnetic relaxation would be strictly exponential in time. In reality the relaxation deviates from the exponential in the kelvin range and is clearly nonexponential in the subkelvin range [5,6].

In this Letter we show that dislocations, undoubtedly present in Mn$_{12}$ crystals, provide long range deformations (see Fig. 1) which should be the main source of spin tunneling. Local rotations of the anisotropy axes due to dislocations are responsible for odd tunneling resonances. Broad distribution of deformations causes broad distribution of tunneling rates. We compute the relaxation law in a crystal with dislocations and show that it obeys scaling that can be tested in experiment.

We study Hamiltonian

$$\mathcal{H} = -DS_z^2 - H_z S_z + \mathcal{H}_{me}, \qquad (1)$$

where S_z is the z component of the spin operator, $S = 10$, $D = 0.65$ K, H_z is the magnetic field applied along the z axis (c axis of the crystal), and $\mathcal{H}_{me}$ is the magnetoelastic coupling. The Hamiltonian of Mn$_{12}$ also contains crystal fields of fourth order on the spin operator, magnetic dipole interactions, and hyperfine interactions. We neglect them in order to emphasize the effect of dislocations and use [10,12]
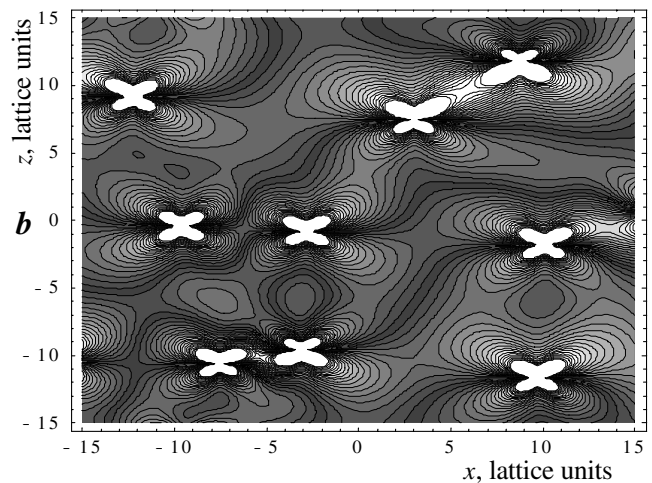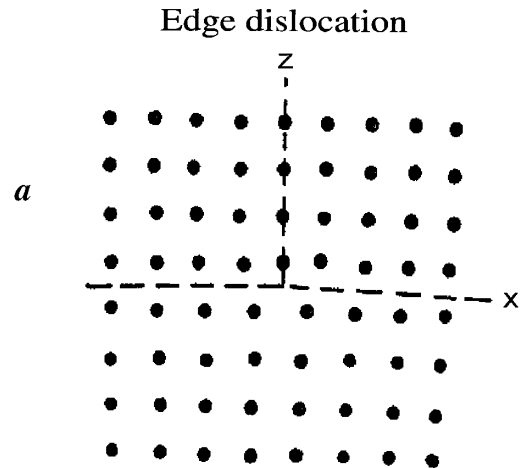

FIG. 1. (a) Edge dislocation with the axis along the Y direction and the extra plane in the positive Z direction; (b) contour plot of the strength of the transverse anisotropy E of Eq. (5) created by a randomized array of dislocations.

$$\mathcal{H}_{me} = g_1 D(\varepsilon_{xx} - \varepsilon_{yy})(S_x^2 - S_y^2) + g_2 D\varepsilon_{xy}\{S_x, S_y\}$$
$$+ g_3 D(\varepsilon_{xz}\{S_x, S_z\} + \varepsilon_{yz}\{S_y, S_z\})$$
$$+ g_4 D(\omega_{xz}\{S_x, S_z\} + \omega_{yz}\{S_y, S_z\}), \quad (2)$$

where

$$\epsilon_\alpha\beta = \frac{1}{2}\left(\frac{\partial u_\alpha}{\partial x_\beta} + \frac{\partial u_\beta}{\partial x_\alpha}\right), \qquad \omega_{\alpha\beta} = \frac{1}{2}\left(\frac{\partial u_\alpha}{\partial x_\beta} - \frac{\partial u_\beta}{\partial x_\alpha}\right) \quad (3)$$

are linear deformation tensors, with **u** being the displacement.

The full classification of relevant elastic deformations due to different types of dislocations will be done elsewhere. In this Letter, we will illustrate the effect of static deformations on tunneling by considering a typical example of edge dislocations running along the y axis, perpendicular to the anisotropy direction (see Fig. 1a) [13]. For the YZ extra crystallographic plane inserted at $z > 0$ one obtains (see, e.g., Ref. [14]) $\varepsilon_{xy} = \varepsilon_{yz} = \omega_{yz} = 0$,

$$\varepsilon_{xz} = \frac{a}{2\pi}\frac{x}{x^2 + z^2}, \qquad \omega_{xz} = \frac{a}{4\pi}\frac{x(x^2 - z^2)}{(1 - \sigma)(x^2 + z^2)^2},$$
$$\varepsilon_{xx} - \varepsilon_{yy} = \frac{a}{4\pi}z\frac{(2\sigma - 3)(x^2 + z^2) + 2z^2}{(1 - \sigma)(x^2 + z^2)^2}, \quad (4)$$

where $0 < \sigma < 1/2$ is the Poisson elastic coefficient (we will use $\sigma = 0.25$). If the extra plane is inserted at $z < 0$, the above expressions change their sign.

Because of the terms of the type $S_x S_z$, etc., in the Hamiltonian, the local easy axis deviates from the z direction. In a locally rotated coordinate system (x', y', z') that restores the normal form of the crystal field, saving terms linear on deformation, one obtains

$$\mathcal{H} = -DS_{z'}^2 - H_z S_{z'} + E(S_{x'}^2 - S_{y'}^2) - H_{x'}S_{x'}, \quad (5)$$

where

$$E = g_1 D(\varepsilon_{xx} - \varepsilon_{yy}), \qquad H_{x'} = \frac{1}{2}(g_3\varepsilon_{xz} + g_4\omega_{xz})H_z. \quad (6)$$

A few observations are in order. Dislocation generates the transverse anisotropy of strength E that decays as $1/r$ [see Eq. (4)] on the distance from the dislocation core. Because of the slow decay of E, a single dislocation produces spin tunneling at a large number of crystal sites. According to Eq. (6) the field applied along the c axis of the crystal generates the transverse field due to the local rotation of the easy axis by the dislocation.

For numerical work we choose $g_1 = g_2 = g_3 = g_4 = 1$ (see, e.g., Ref. [11] and references therein). Figure 1b shows a typical pattern of the transverse anisotropy produced by an array of edge dislocations, obtained by randomization of the quadratic lattice of dislocations with alternating orientation of the extra plane.

Because of the dislocations the local energy barrier between spin-up and spin-down states is lower than in the

ideal crystal. It can be calculated perturbatively from Eq. (5). In addition to the barrier reduction for a classical spin, the barrier in the quantum case is further lowered at the discrete values of H_z,

$$H_{zk} = k\sqrt{D^2 - E^2}, \qquad k = 0, \pm 1, \ldots, \pm 2S \quad (7)$$

that provide resonant tunneling between matching spin levels m and $m' = -m - k$ [4,9,15]. At $H_z = H_{zk}$ the effective height of the barrier,

$$U^{eff} = D(S^2 - m_b^2) - H_z(S + m_b), \quad (8)$$

is determined by $m = m_b < 0$ that corresponds to the lowest pair of levels, m and m', whose tunneling splitting, $\Delta_{mm'}$, is greater than the sum of their widths, $\Gamma_{mm'} = \Gamma_m + \Gamma_{m'}$. Equation (8), even though it accounts for only one tunneling pair of levels, is a good approximation for the relaxation problem (see discussion after Eq. (5.15) and Fig. 5 of Ref. [9]). The splitting is determined by high powers of E and $H_{x'}$, and, thus, strongly depends on coordinates [see Eq. (2.6) of Ref. [9] for the effect of the transverse field and Eq. (4) of Ref. [16] for the effect of transverse anisotropy]. Consequently, the dependence of m_b on $\Gamma_{mm'}$ is weak. In the kelvin range we will use the experimental value $\Gamma_{mm'} \simeq 200$ Oe [17].

To illustrate the barrier reduction by dislocations in the thermally activated regime (kelvin range), we numerically diagonalized Eq. (5) for the 100×100 Mn$_{12}$ lattice around a single edge dislocation at $T = 2$ K and $H = 0$. We determine tunneling levels m_b and the effective barriers U_i^{eff} from Eq. (8) for all sites i of the pattern and construct the relaxation curve

$$R(t) = \frac{1}{N}\sum_i \exp(-\alpha_i t/\tau), \quad (9)$$

where $\alpha_i = e^{(U_\infty - U_i^{eff})/T}$, $U_\infty \equiv DS^2$ is the unperturbed barrier, and $\tau = \tau_0 e^{U_\infty/T}$ is the relaxation time far from the dislocation. One can see from Fig. 2 that the effect of dislocations on relaxation is profound. Even for one dislocation per 100×100 sites in the XZ plane, which corresponds to the concentration of dislocations as small as $c = 10^{-4}$, more than half of the Mn$_{12}$ molecules relax faster than in the ideal crystal.

At temperatures below 1 K, where spin relaxation occurs via tunneling from the ground state, the influence of dislocations becomes even more dramatic. In contrast to the small barrier reduction in the thermally activated regime, here the role of dislocations is to provide the main source of spin relaxation. The resulting level splittings are distributed over many decades. Figure 3a shows distributions of the ground-state level splittings obtained numerically for a randomized array of edge dislocations with concentration $c = 10^{-2}$ for $k = 0$ and $k = 8$ resonances. Since outside dislocation cores the perturbations of the uniaxial Hamiltonian are small, one can scale the splitting distributions for even values of k using the perturbative Eq. (4) of Ref. [16] for the ground-state splitting $(m = -S, m' = -m - k = S - k)$,
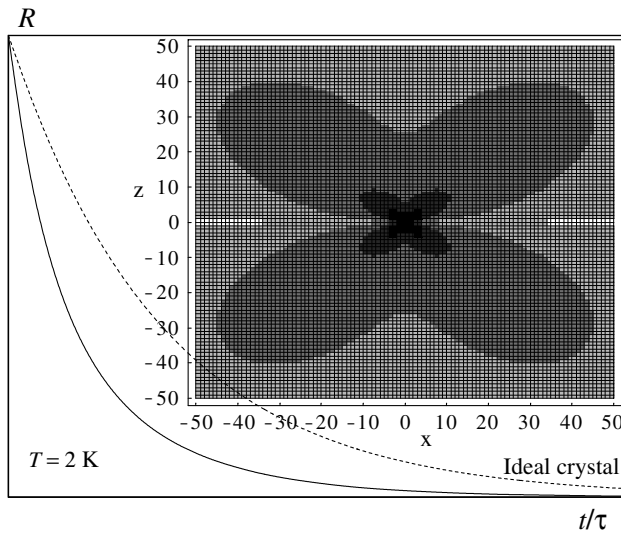
FIG. 2. Relaxation curves for the 100×100 Mn_{12} lattice around a single edge dislocation along the y axis at $T = 2$ K and $H = 0$. Faster relaxation of Mn_{12} molecules caused by the dislocation leads to a nonexponential form of $R(t/\tau)$, where τ is the relaxation time for an ideal sample. Dashed line: Pure thermal exponential in the ideal Mn_{12} crystal. Inset: Tunneling levels $m_b = 0$, -1, -2, -3, and -4 at different points of the lattice ($m_b = 0$ in the small lightmost regions corresponds to the 65 K barrier in an ideal crystal).

$$\Delta_{ki} = g_k \left(\frac{E_i}{8D} \right)^{S-k/2}, \qquad (10)$$

where

$$g_k = \frac{8D}{[(S - k/2 - 1)!]^2} \sqrt{\frac{(2S - k)! \, (2S)!}{k!}}. \qquad (11)$$

Then the distribution of $\ln(\Delta_{ki}/g_k)/(S - k/2) = E_i/(8D)$ does not depend on k; see Fig. 3b. For $k \neq 0$ there is also a transverse field $H_{x'}$ in addition to the transverse anisotropy E in Eq. (5), which should modify Eq. (10). This modification, however, is small away from the dislocation cores. A more significant effect of the transverse field generated by the dislocations is unfreezing of tunneling resonances with odd values of k.

Let us study now spin relaxation produced by sweeping the field H_z through a tunneling resonance. The population of the metastable state with $m = -S$ obeys [9]

$$\dot{N}_{-S} = -\frac{\Delta^2}{2} \frac{\Gamma}{(\varepsilon_{-S} - \varepsilon_{S-k})^2 + \Gamma^2} N_{-S}, \qquad (12)$$

where $\varepsilon_{-S} - \varepsilon_{S-k} = v_k t$ and $v_k \equiv (2S - k) dH_z/dt$. Integrating this equation one obtains the probability for the molecule to remain in the metastable well after crossing the resonance, $P = \exp[-\pi\Delta^2/(2v_k)]$, which coincides with the Landau-Zener formula. The relaxation curve $R(v_k)$ for a sample with dislocations

$$R(v_k) = \frac{1}{N} \sum_i \exp[-\pi\Delta_i^2/(2v_k)] \qquad (13)$$

at different resonances k is shown in Fig. 4. At odd k relaxation is produced by the transverse field $H_{x'}$ in combi-
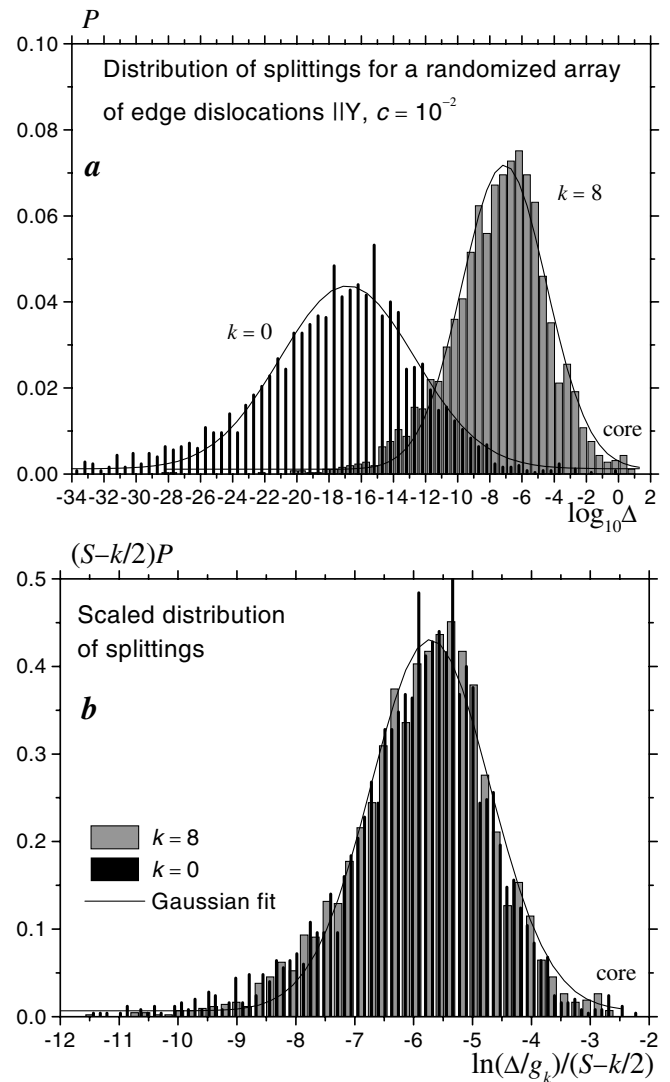

FIG. 3. (a) Distribution of level splittings (in kelvin) created by a randomized array of edge dislocations with $c = 10^{-2}$ for resonances with $k = 0$ and $k = 8$; (b) scaled representation with g_k of Eq. (11).

nation with the transverse anisotropy. For $k = 1$ the effect of $H_{x'}$ is still small and the corresponding relaxation curve is noticeably shifted to the right. Because of the wide distribution of splittings, the sweeping rate needed to make different Mn_{12} molecules to relax stretches over many decades. Consequently, $R(v_k)$ can be plotted only on the log scale. On that scale any individual exponential becomes a step function, $\exp[-\pi\Delta_i^2/(2v_k)] \Rightarrow \theta[1 - \pi\Delta_i^2/(2v_k)]$. Since $R(v_k)$ represents the fraction of Mn_{12} molecules which have $\pi\Delta_i^2 < 2v_k$ and, thus, do not relax, $R(v_k)$ and the distribution of splittings are related as the integral and the derivative. Correspondingly, $R(v_k)$ for different k can be scaled the same way as in Fig. 3b. Deviations from the perfect scaling in Fig. 4b are due to the transverse field.

The effect of dislocations, even at moderate concentrations, appears to be much stronger than the effect of transverse fields $H_\perp$ from nuclear spins and dipole interactions. Simple arguments of the perturbation theory show that the
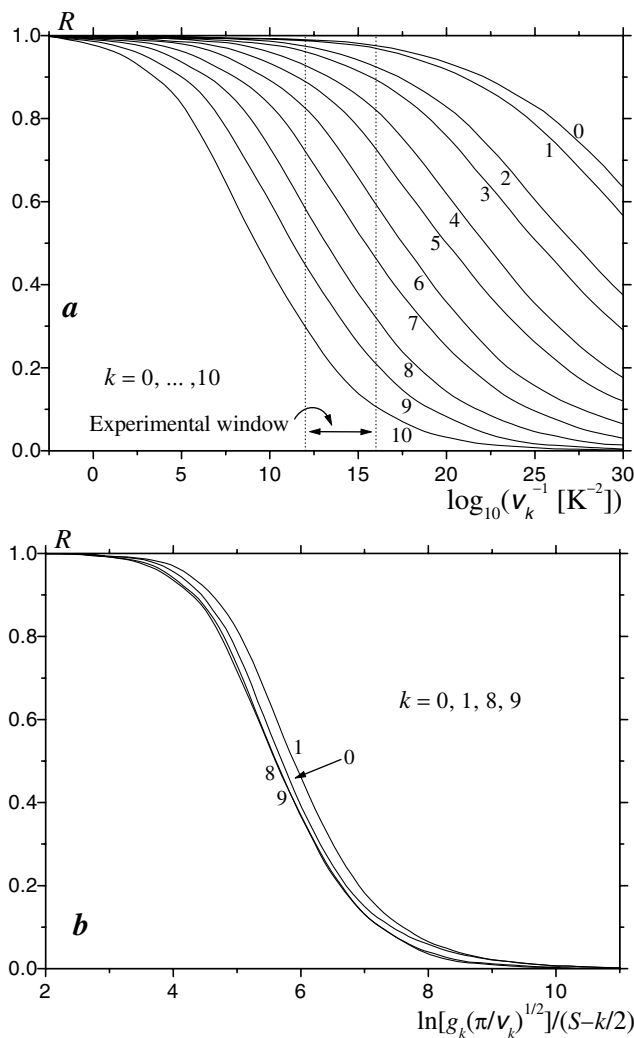
FIG. 4. (a) Spin relaxation as a function of the field sweep rate $v_k = (2S - k)dH_z/dt$ for a randomized array of edge dislocations with $c = 10^{-2}$ at different tunneling resonances k. (b) Scaled representation with g_k of Eq. (11). dH_z/dt is measured in $K^2 \simeq 10^{11}$ T/s.

effect of dislocations becomes comparable with that of $H_\perp$ at $E \sim H_\perp^2/(DS^2)$. With the help of Eqs. (4) and (6) one finds that for $c > 10^{-6}$ the effect of dislocations on tunneling is greater than the effect of hyperfine and dipole fields at almost all crystal sites.

We have shown that dislocations in Mn_{12} crystals should be the main source of spin tunneling in the kelvin and subkelvin temperature range. Local rotations of the easy axes due to dislocations give rise to the effective transverse field which unfreezes odd resonances. Tunneling lifetimes due to dislocations are spread over many decades, which results in the stretched relaxation, especially pronounced in the subkelvin range. Distribution of the tunneling rates and the relaxation law obey scaling which does not depend on the type of crystal defect. That scaling should be seen in experiment. Eventually, it may also become possible to observe magnetization patterns on the surface of Mn_{12}

crystals, shown in Fig. 1. Similar effects must exist in the Fe_8 molecular nanomagnet where dislocations may explain the odd tunneling resonances. The effect of dislocations on even resonances in Fe_8 should be less pronounced, however, because of its strong transverse magnetocrystalline anisotropy.

Note added.— After this Letter was submitted, four groups [18–21] informed us about experimental evidence of the effects discussed here.

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